

# Preparation, crystal structure and chemical bonding analysis of the new binary compounds $\text{Rh}_4\text{Ga}_{21}$ and $\text{Rh}_3\text{Ga}_{16}$

Magnus Boström\*, Yurii Prots, Yuri Grin

Max-Planck-Institut für Chemische Physik fester Stoffe, Nöthnitzer Straße 40, 01187 Dresden, Germany

Received 25 March 2006; accepted 27 April 2006

Available online 9 May 2006

## Abstract

The two new binary compounds  $\text{Rh}_4\text{Ga}_{21}$  (space group  $Cmca$  ( $Cmce$ ),  $a = 40.135(6) \text{ \AA}$ ,  $b = 6.470(2) \text{ \AA}$ ,  $c = 6.473(1) \text{ \AA}$ , Pearson symbol  $oC136$ ) and  $\text{Rh}_3\text{Ga}_{16}$  (space group  $Ccca$  ( $Ccce$ ),  $a = 30.424(7) \text{ \AA}$ ,  $b = 6.476(2) \text{ \AA}$ ,  $c = 6.468(2) \text{ \AA}$ , Pearson symbol  $oC76$ ) were synthesised and their crystal structures were solved from single-crystal X-ray diffraction data. From a topological point of view, both these two crystal structures and the crystal structure of  $\text{PdGa}_5$  can be described either as inhomogeneous intergrowth structures containing three different kinds of segments, or as built up by layers of capped square antiprisms condensed via their capping atoms. Bonding analysis with bonding indicators revealed that the crystal structures of  $\text{Rh}_4\text{Ga}_{21}$  and  $\text{Rh}_3\text{Ga}_{16}$  have to be considered as framework polyanions formed by covalently bonded gallium atoms with embedded rhodium cations.

© 2006 Elsevier Inc. All rights reserved.

**Keywords:** Binary compound; Rhodium; Gallium; Crystal structure; Electron localization function; Electron localizability indicator

## 1. Introduction

Four binary phases are known in the Rh–Ga system;  $\text{RhGa}$  (CsCl type, Pearson symbol  $cP2$ ) [1],  $\text{Rh}_{10}\text{Ga}_{17}$  (prototype,  $tP108$ ) [2],  $\text{RhGa}_3$  (IrIn<sub>3</sub> type [3],  $tP16$ ) [4] and  $\text{Rh}_2\text{Ga}_9$  (prototype,  $mP22$ ) [5,6]. No phase diagram has hitherto been published. In course of a systematic investigation of Ga- and Al-rich compounds of Ir, several new phases were found [6,7]. This encouraged an investigation of the chemically related Rh–Ga system, of which the first results are the subject of the present work.

## 2. Experimental

Single crystals of  $\text{Rh}_4\text{Ga}_{21}$  were prepared in a Ga-rich self-flux containing 0.0538 g Rh (99.9%, Chempur) and 0.952 g Ga (99.999%, Chempur), hence having the nominal composition  $\text{Rh}_{3.7}\text{Ga}_{96.3}$ . The elements were sealed inside an evacuated quartz tube already prepared with a quartz wool filter on a support of small pieces of crushed quartz

glass according to the high-temperature centrifugation aided filtration technique (HTCAF) [8,9]. The sample was heat treated at 300 °C for 18 days before the melt was removed from the solid using a centrifuge operating at 2000g, without significantly decreasing the temperature of the sample.

Single crystals of  $\text{Rh}_3\text{Ga}_{16}$  were prepared analogously from 0.0239 g Rh and 1.003 g Ga (nominal composition  $\text{Rh}_{1.6}\text{Ga}_{98.4}$ ), but cooled down from 900 °C at the rate of 5 °C/h down to 150 °C, where the sample was kept for 18 days before the melt was removed.

X-ray powder diffraction patterns of the powdered single crystals were collected with a Huber Imaging Plate Guinier Camera 670 using  $\text{CuK}\alpha_1$  radiation ( $\lambda = 1.54059 \text{ \AA}$ ) for  $\text{Rh}_3\text{Ga}_{16}$  and  $\text{CoK}\alpha_1$  radiation ( $\lambda = 1.78897 \text{ \AA}$ ) for  $\text{Rh}_4\text{Ga}_{21}$ . Silicon ( $a = 5.43119(1) \text{ \AA}$ ) and  $\text{LaB}_6$  powder ( $a = 4.15692(1) \text{ \AA}$ ), respectively, were added as internal standard to the samples. The lattice parameters were refined from the powder data with the program CELLREF [10].

Single crystals with well-exhibited faces were isolated and parts of them were used for the X-ray diffraction experiment. Single-crystal X-ray diffraction data were

\*Corresponding author. Fax: +49 351 4646 4002.

E-mail address: [bostroem@cphys.mpg.de](mailto:bostroem@cphys.mpg.de) (M. Boström).

collected on a Rigaku Mercury CCD diffraction system employing MoK $\alpha$  radiation ( $\lambda = 0.71069 \text{ \AA}$ ). The measured data sets were corrected for absorption using multi-scans in the Laue-class *mmm*. Relevant details for the data collection and handling are summarized in Table 1.

The crystal structures of Rh<sub>4</sub>Ga<sub>21</sub> and Rh<sub>3</sub>Ga<sub>16</sub> were solved by direct methods with the Shelxs97 program [11]. The refinement was performed using the program Jana2000 [12]. The refined parameters were scale factor, atomic coordinates, anisotropic displacement parameters, extinction coefficient and a twinning factor for Rh<sub>3</sub>Ga<sub>16</sub>.

The TB–LMTO–ASA program package [13] with exchange correlation potential (LDA) according to Barth and Hedin [14] was used for quantum chemical calculations. Because of the clear similarity between the crystal structures of Rh<sub>3</sub>Ga<sub>16</sub> and Rh<sub>4</sub>Ga<sub>21</sub>, the calculations were made only for the latter. The radial scalar-relativistic Dirac equation was solved to obtain the partial waves. A calculation within the atomic sphere approximation (ASA) includes corrections for the neglect of partial waves

of higher order and interstitial regions [15], hence no addition of empty spheres was found to be necessary. The radii of the atomic spheres used in the calculations were:  $r(\text{Rh}1) = 1.609 \text{ \AA}$ ,  $r(\text{Rh}2) = 1.630 \text{ \AA}$ ,  $r(\text{Ga}1) = 1.543 \text{ \AA}$ ,  $r(\text{Ga}2) = 1.537 \text{ \AA}$ ,  $r(\text{Ga}3) = 1.579 \text{ \AA}$ ,  $r(\text{Ga}4) = 1.581 \text{ \AA}$ ,  $r(\text{Ga}5) = 1.605 \text{ \AA}$ ,  $r(\text{Ga}6) = 1.597 \text{ \AA}$ ,  $r(\text{Ga}7) = 1.571 \text{ \AA}$ . A basis set containing the Rh(5s, 5p, 4d) and Ga(4s, 4p) orbitals was employed for the self-consistent calculations with the Rh(4f) and Ga(4d) functions being downfolded. The electron localization function (ELF,  $\eta$ ) was evaluated according to [16] within the TB–LMTO–ASA program package with an ELF module already implemented. To gain a deeper insight in the chemical bonding, the topology of ELF was analysed with the program Basin [17]. The electron density was integrated in basins which were bound by zero flux surfaces in the ELF gradient. This method, analogous to the procedure proposed by Bader [18] for charge calculations from electron densities resulted in electron counts for each basin, which revealed basic information for the description of the bonding situation.

Table 1  
Crystallographic information and data handling for Rh<sub>4</sub>Ga<sub>21</sub> and Rh<sub>3</sub>Ga<sub>16</sub>

Crystal data	Rh <sub>4</sub> Ga <sub>21</sub>	Orthorhombic	Rh <sub>3</sub> Ga <sub>16</sub>
Chemical formula	Rh <sub>4</sub> Ga <sub>21</sub>		Rh <sub>3</sub> Ga <sub>16</sub>
Crystal system		Orthorhombic	
Space group	<i>Cmca</i> ( <i>Cmce</i> )		<i>Ccca</i> ( <i>Ccce</i> )
Z	4		4
<i>a</i> (Å) <sup>a</sup>	40.135(6)		30.424(7)
<i>b</i> (Å) <sup>a</sup>	6.470(2)		6.476(2)
<i>c</i> (Å) <sup>a</sup>	6.473(1)		6.468(2)
<i>V</i> (Å <sup>3</sup> ) <sup>a</sup>	1681		1274
Density calc. (g cm <sup>-3</sup> )	7.41		7.42
Crystal form		Irregular	
Crystal size (mm <sup>3</sup> )	0.050 × 0.040 × 0.020		0.040 × 0.030 × 0.015
Colour		Grey metallic	
Absorption coefficient (mm <sup>-1</sup> )	36.8		37.0
Data collection			
Diffraction system		Rigaku AFC7 Mercury CCD	
Radiation, $\lambda$ (Å)		MoK $\alpha$ , 0.71069	
No. of measured reflections	6820		2858
Range of <i>hkl</i>	$-43 \leq h \leq 57$ $-9 \leq k \leq 9$ $-8 \leq l \leq 8$		$-41 \leq h \leq 41$ $-8 \leq k \leq 7$ $-6 \leq l \leq 8$
Absorption correction		Multi-scan	
<i>T</i> <sub>min</sub> / <i>T</i> <sub>max</sub>	0.523		0.541
<i>R</i> <sub>int</sub>	0.055		0.045
Refinement			
Refinement on		<i>F</i>	
No. of independent reflections	1286		759
No. of independent observed reflections	967		565
Observation criterion		<i>I</i> > 3 $\sigma$ ( <i>I</i> )	
No. of reflections used in refinement	1286		759
No. of parameters refined	62		47
Weighting scheme		Unit	
<i>R</i> ( <i>F</i> ) <sub>all</sub> , w <i>R</i> ( <i>F</i> ) <sub>all</sub> , <i>R</i> ( <i>F</i> ) <sub>obs</sub>	0.053, 0.046, 0.036		0.076, 0.061, 0.060
<i>GOF</i> <sub>all</sub>	1.0		5.0
$\Delta\rho_{\text{max}}$ , $\Delta\rho_{\text{min}}$ , (e Å <sup>-3</sup> )	2.0, -1.8		6.2, -1.9
Extinction model	Gaussian isotropic		—
Extinction coefficient	0.051(2)		—

<sup>a</sup>Cell parameters from powder diffraction data with internal standard.

### 3. Results and discussion

The crystal structure of  $\text{Rh}_4\text{Ga}_{21}$  was successfully solved by direct methods and refined in the space group  $Cmca$  ( $Cmce$ ). Final residual values and further details on the refinement are listed in Table 1. Final coordinates and atomic displacement parameters are summarized in Tables 2 and 3. The interatomic distances are listed in Table 4.

Direct methods failed to solve the crystal structure of  $\text{Rh}_3\text{Ga}_{16}$ , apparently due to twinning. Since the two shorter lattice parameters are practically identical for  $\text{Rh}_4\text{Ga}_{21}$  and  $\text{Rh}_3\text{Ga}_{16}$ , it was assumed that the structures ought to be closely related. The long  $a$ -axis of  $\text{Rh}_3\text{Ga}_{16}$  is very close to  $3/4$  of the corresponding axis in  $\text{Rh}_4\text{Ga}_{21}$ . A hypothetical structure model was constructed with slabs containing three layers of condensed capped square antiprisms (instead of four as in the structure of  $\text{Rh}_4\text{Ga}_{21}$ ) but otherwise completely analogous to the structure of  $\text{Rh}_4\text{Ga}_{21}$  (Fig. 1). The hypothetical structure was constructed in the space group  $P1$ , whereafter the highest reasonable space group  $Cmca$  ( $Ccce$ ) was established using symmetry analysis using the program Platon [19] in several steps together with refinement. The twinning relation is described by a diagonal mirror plane represented by the matrix

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}.$$

Table 2  
Final atomic parameters for  $\text{Rh}_4\text{Ga}_{21}$

Atom	Site	$x$	$y$	$z$	$U_{\text{eq}}^a$
Rh1	8	0.43958(2)	0	0.5	0.0065(2)
Rh2	8	0.31831(2)	0	0.5	0.0076(2)
Ga1	4	0.5	0	0.5	0.0194(6)
Ga2	8	0.37924(4)	0	0.5	0.0196(5)
Ga3	8	0.25693(4)	0	0.5	0.0238(5)
Ga4	16	0.46565(3)	0.3504(2)	0.3505(2)	0.0125(3)
Ga5	16	0.41443(3)	0.3484(2)	0.6516(2)	0.0128(3)
Ga6	16	0.34701(3)	0.3537(2)	0.6456(2)	0.0131(3)
Ga7	16	0.29621(3)	0.3391(2)	0.3386(2)	0.0159(3)

$$^a U_{\text{eq}} = 1/3 \sum_i \sum_j U_{ij} a_i^* a_j^* a_i a_j.$$

Table 3  
Anisotropic atomic displacement parameters for  $\text{Rh}_4\text{Ga}_{21}$ <sup>a</sup>

Atom	$U_{11}$	$U_{22}$	$U_{33}$	$U_{12}$	$U_{13}$	$U_{23}$
Rh1	0.0052(4)	0.0069(4)	0.0076(4)	0	0	−0.0002(3)
Rh2	0.0060(4)	0.0091(4)	0.0076(4)	0	0	0.0005(3)
Ga1	0.0046(8)	0.024(2)	0.029(1)	0	0	0.001(1)
Ga2	0.0056(6)	0.0249(8)	0.0281(9)	0	0	0.0015(7)
Ga3	0.0049(7)	0.036(1)	0.0308(9)	0	0	−0.0056(8)
Ga4	0.0122(5)	0.0121(5)	0.0131(5)	−0.0002(4)	−0.0003(4)	0.0025(4)
Ga5	0.0117(5)	0.0136(5)	0.0131(5)	0.0000(4)	−0.0003(4)	−0.0022(4)
Ga6	0.0108(5)	0.0140(5)	0.0144(5)	0.0000(4)	0.0001(4)	−0.0002(4)
Ga7	0.0196(6)	0.0147(5)	0.0135(5)	0.0050(4)	0.0047(4)	0.0050(4)

<sup>a</sup>The total displacement factor is calculated as  $\exp[-2\pi^2(U_{11}h^2a^{*2} + U_{22}k^2b^{*2} + U_{33}l^2c^{*2} + U_{12}hka^*b^* + U_{13}hla^*c^* + U_{23}klb^*c^*)]$ .

The subsequent successful refinement verified the correctness of the model. For  $\text{Rh}_3\text{Ga}_{16}$ , the same parameters were refined as for the  $\text{Rh}_4\text{Ga}_{21}$  structure, except for that no extinction was refined. An additional parameter for twinning was refined to be 0.353(9). Further details of the

Table 4  
Interatomic distances in  $\text{Rh}_4\text{Ga}_{21}$

Atoms	Distance (Å)
Rh1–Ga1	2.4251(9)
Rh1–Ga2	2.421(2)
Rh1–Ga4	2.678(1)
Rh1–Ga4	2.679(1)
Rh1–Ga5	2.658(1)
Rh2–Ga2	2.446(2)
Rh2–Ga3	2.463(2)
Rh2–Ga6	2.730(1)
Rh2–Ga6	2.736(1)
Rh2–Ga7	2.587(1)
Rh2–Ga7	2.583(1)
Ga1–Ga4	2.824(1)
Ga1–Ga4	2.825(1)
Ga2–Ga5	2.835(1)
Ga2–Ga5	2.836(1)
Ga2–Ga6	2.792(1)
Ga2–Ga6	2.798(1)
Ga3–Ga7	2.896(1)
Ga3–Ga7	2.593(2)
Ga3–Ga7	2.893(1)
Ga4–Ga4	2.757(2)
Ga4–Ga4	2.738(2)
Ga4–Ga5	2.833(2)
Ga4–Ga5	2.745(2)
Ga5–Ga5	2.775(2)
Ga5–Ga6	2.706(2)
Ga6–Ga6	2.672(2)
Ga6–Ga7	2.849(2)
Ga6–Ga7	2.850(2)
Ga6–Ga7	2.697(2)
Ga7–Ga7	2.950(2)

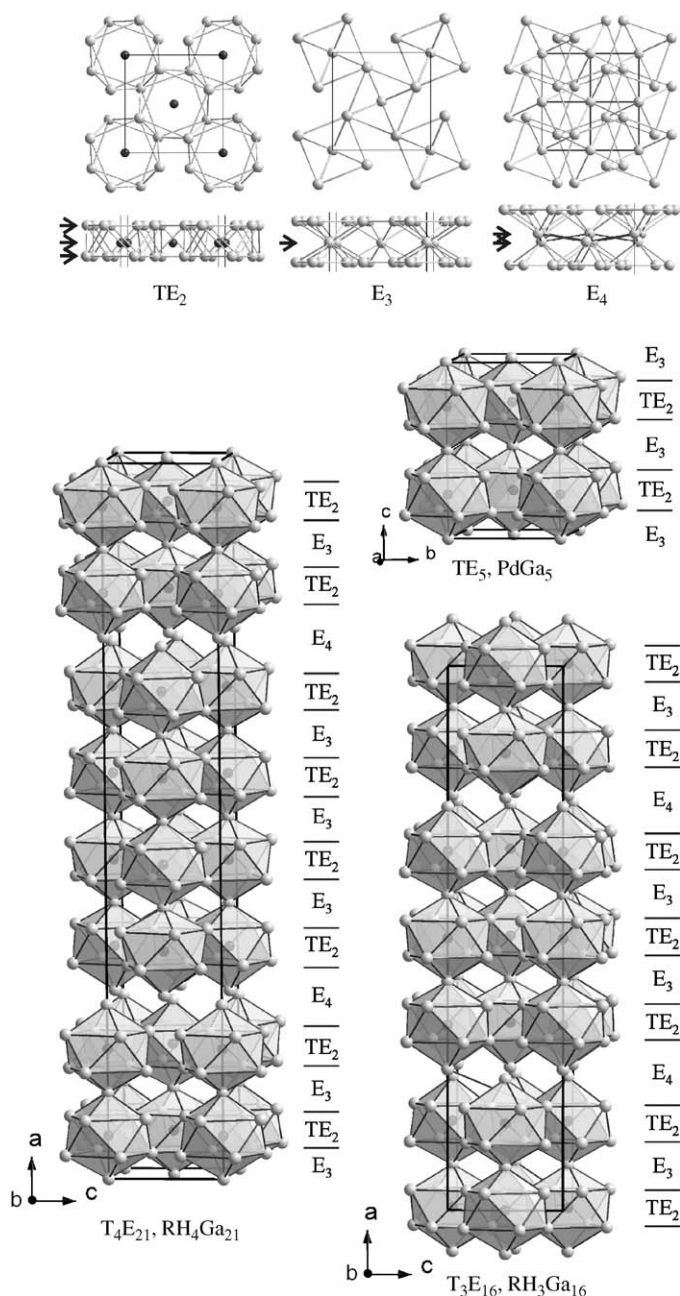


Fig. 1. Three kinds of structural segments (top) and crystal structures of PdGa<sub>5</sub>, Rh<sub>4</sub>Ga<sub>21</sub> and Rh<sub>3</sub>Ga<sub>16</sub> as intergrowth derivatives (bottom) Arrangement of condensed capped antiprisms [PdGa<sub>10</sub>] are highlighted. The arrows indicate which atoms are considered in the segment formulas.

refinement and final atomic parameters are summarized in Tables 5 and 6. The corresponding interatomic distances are found in Table 7.

Both crystal structures, Rh<sub>3</sub>Ga<sub>16</sub> and Rh<sub>4</sub>Ga<sub>21</sub>, represent new structure types for intermetallic compounds. They can both be related to the archetype PdGa<sub>5</sub> [3,20], (space group *I4/mcm*,  $a = 6.436(6)$  Å,  $c = 9.990(8)$  Å, Pearson symbol *tI10*), cf. Fig. 1. This group of intermetallic compounds can be interpreted within the concept of intergrowth structures [21–23]. In this case three different

Table 5  
Final atomic parameters for Rh<sub>3</sub>Ga<sub>16</sub>

Atom	Site	$x$	$y$	$z$	$U_{\text{eq}}^a$
Rh1	4	0	0.5	0	0.0072(8)
Rh2	8	0.15982(4)	0.5	0	0.0102(7)
Ga1	8	0.07958(6)	0.5	0	0.020(2)
Ga2	8	0.24074(7)	0.5	0	0.028(2)
Ga3	16	0.03356(5)	0.3493(3)	0.3483(3)	0.0134(6)
Ga4	16	0.18943(6)	0.3382(3)	-0.3390(3)	0.0194(6)
Ga5	16	0.12236(5)	0.1456(3)	-0.1460(3)	0.0152(6)

$$^a U_{\text{eq}} = 1/3 \sum_i \sum_j U_{ij} a_i^* a_j^*$$

segments are necessary for the complete description of the symmetry, unit cell parameters and composition of the possible intermediate crystal structures, hence this is an example of so-called inhomogeneous intergrowth. The first kind of segments (Fig. 1, top left) has a composition  $2 \times TE_2$  ( $T = \text{transition metal}$ ,  $E = \text{Al or Ga}$ ) and represents half the unit cell of the prototype structure CuAl<sub>2</sub> (space group *I4/mcm*,  $a = 7.067(1)$  Å,  $c = 4.877(1)$  Å, Pearson symbol *tI12*) [24–26]. The second one (Fig. 1, top middle) can be understood as an emptied U<sub>3</sub>Si<sub>2</sub> structure [27]:  $2 \times \text{Si}_2\text{U}_3 \rightarrow 2 \times \square_2 E_3$ . Both mentioned fragments have tetragonal minimal symmetry complex [23], thus the structure containing only these two types of segments (PdGa<sub>5</sub>) is also tetragonal. The last type of the segments (Fig. 1, top right) can also be derived from the structure of U<sub>3</sub>Si<sub>2</sub> and has a composition of  $2 \times E_4$ . Stacking sequences of the segments in the crystal structures of PdGa<sub>5</sub>, Rh<sub>3</sub>Ga<sub>16</sub> and Rh<sub>4</sub>Ga<sub>21</sub> are shown in Fig. 1, bottom. The compositions of the unit cells can be calculated as

$$4TE_2 + 4E_3 = T_4E_{20} = 4TE_5 \text{ for PdGa}_5,$$

$$16TE_2 + 12E_3 + 4E_4 = T_{16}E_{84} = 4T_4E_{21} \text{ for Rh}_4\text{Ga}_{21},$$

$$12TE_2 + 12E_3 + 4E_4 = T_{12}E_{64} = 4T_3E_{16} \text{ for Rh}_3\text{Ga}_{16}.$$

In all three crystal structures discussed above, transition metal atoms have a square antiprismatic environment formed by Ga atoms (Fig. 1). Two additional Ga atoms cap the square faces of the antiprisms, resulting in the coordination number 10 around the rhodium atoms. In the title compounds, the antiprisms are sharing the capping atoms along the stacking axis and in this way form chains. The chains are further condensed sharing a half of the side edges, in the same way as in the PdGa<sub>5</sub> structure type. In the PdGa<sub>5</sub> structure the chains are infinite. The chains in the rhodium gallides are split in three- (Rh<sub>3</sub>Ga<sub>16</sub>) or four-membered (Rh<sub>4</sub>Ga<sub>21</sub>) fragments. The neighboring fragments are shifted by  $(0, \frac{1}{2}, 0)$ . With this kind of description the compositions of the unit cells for PdGa<sub>5</sub>, Rh<sub>3</sub>Ga<sub>16</sub> and Rh<sub>4</sub>Ga<sub>21</sub> can be obtained as

$$[TE_{8/2}^{\text{ap}} E_{2/2}^{\text{s}}]_4 = 4TE_5,$$

Table 6  
Anisotropic atomic displacement parameters for Rh<sub>3</sub>Ga<sub>16</sub><sup>a</sup>

Atom	$U_{11}$	$U_{22}$	$U_{33}$	$U_{12}$	$U_{13}$	$U_{23}$
Rh1	0.0105(7)	0.006(2)	0.005(2)	0	0	0
Rh2	0.0120(5)	0.009(2)	0.009(2)	0	0	0.0004(5)
Ga1	0.0099(8)	0.026(3)	0.024(3)	0	0	0.000(2)
Ga2	0.0109(9)	0.046(3)	0.028(2)	0	0	0.009(2)
Ga3	0.0173(7)	0.011(2)	0.012(2)	0.0009(6)	−0.0014(6)	0.0028(6)
Ga4	0.0263(8)	0.014(2)	0.017(2)	−0.0062(8)	0.0044(7)	−0.0053(6)
Ga5	0.0176(7)	0.013(2)	0.015(2)	0.0002(6)	0.0000(6)	0.0002(6)

<sup>a</sup>The total displacement factor is calculated as  $\exp[-2\pi^2(U_{11}h^2a^{*2} + U_{22}k^2b^{*2} + U_{33}l^2c^{*2} + U_{12}hka^*b^* + U_{13}hla^*c^* + U_{23}klb^*c^*)]$ .

Table 7  
Interatomic distances in Rh<sub>3</sub>Ga<sub>16</sub>

Atoms	Distance (Å)
Rh1–Ga1	2.421(2)
Rh1–Ga3	2.659(2)
Rh1–Ga3	2.669(2)
Rh2–Ga1	2.441(2)
Rh2–Ga2	2.462(2)
Rh2–Ga4	2.591(2)
Rh2–Ga4	2.587(2)
Rh2–Ga5	2.731(2)
Rh2–Ga5	2.726(2)
Ga1–Ga3	2.826(2)
Ga1–Ga3	2.835(2)
Ga1–Ga5	2.802(2)
Ga1–Ga5	2.797(2)
Ga4–Ga4	2.955(3)
Ga4–Ga5	2.697(3)
Ga4–Ga5	2.852(3)
Ga4–Ga5	2.849(3)
Ga5–Ga5	2.669(3)

$$[TE_{8/2}^{ap}E_{2/2}^s]_4[TE_{8/2}^{ap}E_{1/2}^sE^{us}]_8 = 4T_3E_{16},$$

$$[TE_{8/2}^{ap}E_{2/2}^s]_8[TE_{8/2}^{ap}E_{1/2}^sE^{us}]_8 = 4T_4E_{21},$$

where the denominator 2 implies that the atom is shared; ap = antiprism, s = shared apex, us = unshared apex. Breaking the chains together with a shift along [010] and/or [001] (coordinate system of Rh<sub>3</sub>Ga<sub>16</sub> and Rh<sub>4</sub>Ga<sub>21</sub>) leads to a reduction of the total symmetry from tetragonal to orthorhombic and is obviously the reason for twinning of the single crystals of Rh<sub>3</sub>Ga<sub>16</sub>. Nevertheless the two shorter lattice parameters in both the rhodium gallides are equal within 2 standard deviations.

The chain arrangement of TE<sub>10</sub> polyhedra results in the formation of “empty” space between the chains. In the PdGa<sub>5</sub> as well as in the CuAl<sub>2</sub> structures, a covalent

interaction between the antiprisms takes place in this “empty” space [26,28]. This was taken as a starting point for the bonding analysis of the compounds Rh<sub>4</sub>Ga<sub>21</sub> and Rh<sub>3</sub>Ga<sub>16</sub>.

The electron localization function (ELF) was chosen as a suitable tool for this investigation. Originally introduced by Becke and Edgcombe within the Hartree–Fock theory [29] and redefined later by Savin et al. [16] for the density functional theory, the electron localization function belongs to the so-called bonding indicators in real space. Functions of this group trace the correlation of electronic motion of same-spin electrons. A more general functional of this kind is called electron localization indicator (ELI) [30]. ELF (as an approximation of ELI) represents a charge distribution of electron pairs and is thus a suitable tool for analysis of chemical bonding in the sense of Lewis theory, where pair formation plays the central role. Maxima of ELF (and ELI) in the valence region provide signatures for directed (covalent) bonding in real space.

Some of the interatomic Rh–Ga distances (2.41–2.47 Å, Tables 4 and 7) are very short in comparison with the sum of radii ( $r_{\text{met}}(\text{Rh}) = 1.34 \text{ \AA}$ ,  $r_{\text{met}}(\text{Ga}) = 1.22 \text{ \AA}$ ,  $r_{\text{cov}}(\text{Rh}) = 1.25$ ,  $r_{\text{cov}}(\text{Ga}) = 1.25 \text{ \AA}$  [31]). Despite this fact, no unique ELF attractors were found on the Rh–Ga contacts inside the polyhedra in the crystal structure of Rh<sub>4</sub>Ga<sub>21</sub>.

Topological analysis of the electron localization function revealed attractors (function maxima) which were located mostly on the Ga–Ga contacts (two-centre bonds) and can be classified in five different groups (Fig. 2, left). The attractors of the first kind are located in the “empty” space between the gallium atoms of neighboring chains (Ga3–Ga3, Ga4–Ga4 and Ga6–Ga6 bonds), similar to the bonding picture in PdGa<sub>5</sub> and CuAl<sub>2</sub>. Also the second group of attractors was found outside the antiprisms, namely between the unshared Ga atoms capping the antiprisms of neighboring chain fragments (three-centre bonds Ga6–Ga7–Ga6). Attractors of a third kind were observed on the Ga–Ga contacts constituting the side edges between adjacent triangular faces of the antiprisms (two-center bonds Ga3–Ga4, Ga5–Ga6). The next group of attractors is located between capping Ga atoms and

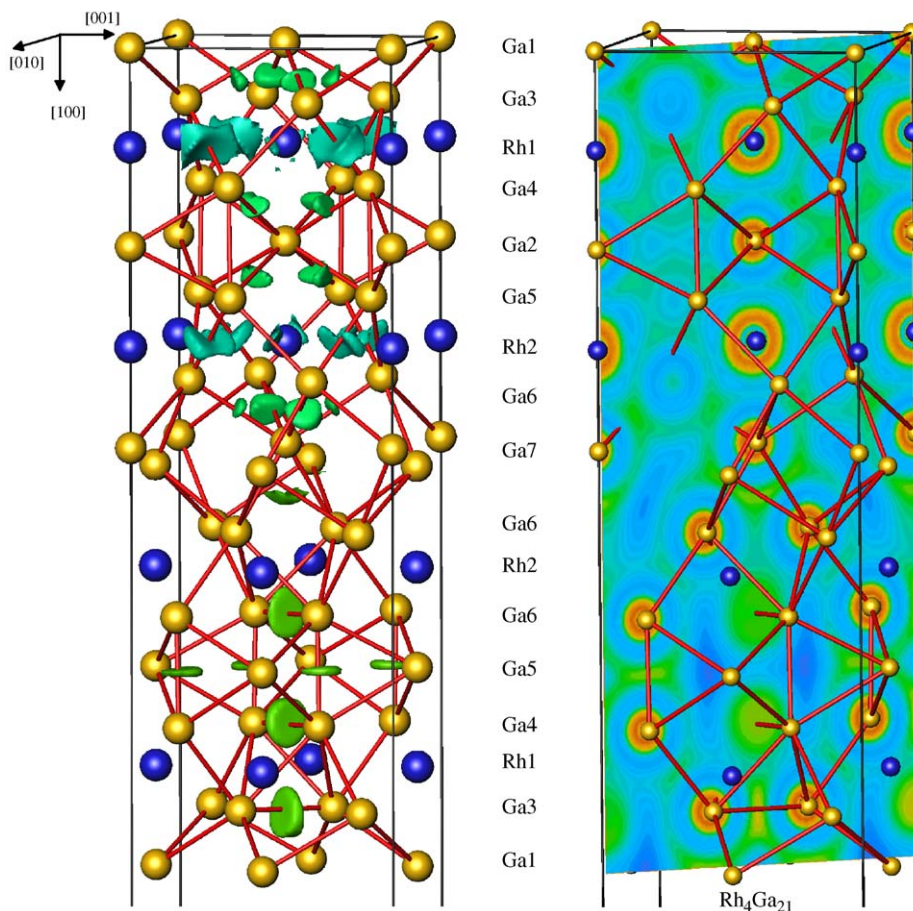


Fig. 2. Electron localization function of the crystal structure of  $Rh_4Ga_{21}$ : (left) isosurfaces of ELF showing the positions of the attractors of the Ga–Ga contacts. (right) ELF distribution on the (011) plane revealing the non-structured spherical topology of ELF in the penultimate shell of rhodium and gallium atoms and the absence of attractors on the Rh–Ga contacts.

Ga atoms on the side edges of the  $[TE_{10}]$  polyhedron (two-center bonds Ga1–Ga3, Ga4–Ga2, Ga2–Ga5, Ga6–Ga7). Attractors of the last group are situated on the bonds between antiprisms belonging to the same chain (Ga4–Ga6 bonds).

Integration of the electron density within the basins of ELF attractors gave counts of  $43.8 \approx 44$  electrons for the inner shells of the crystallographically independent rhodium atoms, indicating the configuration  $Rh^{1+}$ . Based on the ELF/electron density approach, the crystal structures of  $Rh_4Ga_{21}$  and  $Rh_3Ga_{16}$  should be described as a covalently bonded network of Ga atoms forming capped square-antiprismatic cages, each containing a Rh atom (Fig. 3). The interaction between the Rh atoms and the Ga network is rather a Coulomb one, with the valence electrons of Rh transferred to the network according to the balances  $(Rh^{1+})_4(Ga_{21})^{4-}$  or  $(Rh^{1+})_3(Ga_{15})^{3-}$ .

The formation of covalent bonds in the “empty” part of the structure between Ga (Al) atoms (i) belonging to the neighboring antiprisms and (ii) forming the side edges of the antiprisms were also observed in the two archetype structures  $PdGa_5$  and  $CuAl_2$ . However, in contrary to the

case of  $Rh_4Ga_{21}$ , a directed (covalent) interaction between the transition metal (Pd, Ga) and the Ga (Al) atoms was found in the ELF of both  $PdGa_5$  and  $CuAl_2$ .

#### 4. Conclusions

The two new binary compounds  $Rh_4Ga_{21}$  and  $Rh_3Ga_{16}$  were prepared in single-crystalline form and structurally characterized. In both crystal structures, as well as in  $PdGa_5$ , the transition metal atoms are 10-coordinated by gallium. From the bonding analysis, the new compounds are described as framework gallium polyanions with rhodium cations embedded in the tetragonal antiprismatic cavities, according to the electronic balances  $(Rh^{1+})_4(Ga_{21})^{4-}$  or  $(Rh^{1+})_3(Ga_{15})^{3-}$ .

Further details of the crystal structure investigation can be obtained from Fachinformationszentrum Karlsruhe, 76344 Eggenstein-Leopoldshafen, Germany, (fax: +49 7247 808 666; e-mail: [crysdata@fiz.karlsruhe.de](mailto:crysdata@fiz.karlsruhe.de)) on quoting the depository number CSD 415870 for  $Rh_4Ga_{21}$  and CSD 415871 for  $Rh_3Ga_{16}$ .

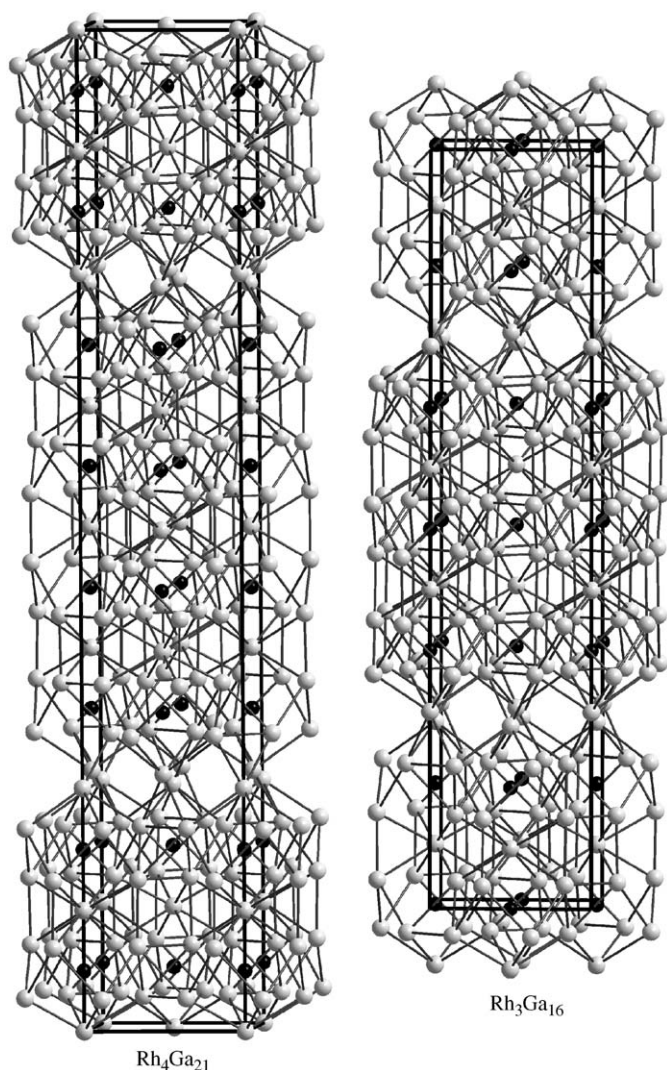


Fig. 3. Anionic gallium frameworks with embedded rhodium cations in the crystal structure of  $\text{Rh}_4\text{Ga}_{21}$  and  $\text{Rh}_3\text{Ga}_{16}$  as revealed by the analysis of the chemical bonding.

## References

- [1] B.H. Verbeek, H.W.A.M. Rompa, P.K. Larsen, M.S. Methfessel, F.M. Mueller, *Phys. Rev. B* 28 (1983) 6774–6779.
- [2] H. Völlenkle, A. Wittmann, H. Nowotny, *Monatsh. Chem.* 98 (1967) 176–183.
- [3] K. Schubert, H.L. Lukas, H.G. Meissner, S. Bhan, *Z. Metallkd.* 50 (1959) 534–540.
- [4] K. Schubert, H. Breimer, R. Gohle, H.L. Lukas, H.G. Meissner, E. Stolz, *Naturwissenschaften* 45 (1958) 360–361.
- [5] L.E. Edshammar, *Acta Chem. Scand.* 24 (1970) 1457–1458.
- [6] M. Boström, H. Rosner, Y. Prots, U. Burkhardt, Y. Grin, *Z. Allg. Anorg. Chem.* 631 (2005) 534–541.
- [7] M. Boström, Y. Prots, Y. Grin, *Solid State Sci.* 6 (2004) 499–503.
- [8] Z. Fisk, J.P. Remeika, in: K.A. Gschneider, L.R. Eyring (Eds.) *Handbook on the Physics and Chemistry of the Rare Earths*, vol. 12, North-Holland, Amsterdam, 1989, p. 53.
- [9] M. Boström, S. Hovmöller, *J. Alloys Compd.* 314 (2001) 154–159.
- [10] J. Laugier, B. Bochu, CELLREF, Laboratoire des Matériaux et du Génie Physique de l'École Supérieure de Physique de Grenoble, France, 2003.
- [11] G.M. Sheldrick, SHELXS97–A Program for Automatic Solution of Crystal Structures, University of Göttingen, Germany, 1997.
- [12] V. Petricek, M. Dusek, Jana2000. The Crystallographic Computing System, Institute of Physics, Praha, Czech Republic, 2000.
- [13] O. Jepsen, A. Burkhardt, O.K. Andersen, The Program TB–LMTO–ASA. Version 4.7, Max-Planck-Institut für Festkörperforschung, Stuttgart, 1999.
- [14] U. Barth, L. Hedin, *J. Phys. C* 5 (1972) 1629–1642.
- [15] O.K. Andersen, *Phys. Rev. B* 12 (1975) 3060–3083.
- [16] A. Savin, H.J. Flad, J. Flad, H. Preuss, H.G. von Schnering, *Angew. Chem.* 104 (1992) 185; A. Savin, H.J. Flad, J. Flad, H. Preuss, H.G. von Schnering, *Angew. Chem. Int. Ed. Engl.* 31 (1992) 185–187.
- [17] M. Kohout, Basin. Version 3.1, Max-Planck-Institut für Chemische Physik fester Stoffe, Dresden, Germany, 2005.
- [18] R.F.W. Bader, *Atoms in Molecules: A Quantum Theory*, Oxford University Press, Oxford, 1999.
- [19] A.L. Spek, *J. Appl. Crystallogr.* 36 (2003) 7–13.
- [20] Yu. Grin, K. Peters, H.G. von Schnering, *Z. Kristallogr. NCS.* 212 (1997) 6.
- [21] Yu. Grin, Ya.P. Yarmolyuk, E.I. Gladyshevski, *Kristallografia* 27 (1982) 686–692; Yu. Grin, Ya.P. Yarmolyuk, E.I. Gladyshevski, *Sov. Phys. Crystallogr.* 27 (4) (1982) 413–418.
- [22] E. Parthé, B. Chabot, K. Cenzual, *Chimia* 39 (1985) 164–174.
- [23] Yu. Grin, in: E. Parthé (Ed.), *Modern Perspectives in Inorganic Crystal Chemistry*, Kluwer Academic Publishers, Dordrecht, The Netherlands, 1992, pp. 77–95.
- [24] J.B. Friauf, *J. Amer. Chem. Soc.* 49 (1927) 3107–3114.
- [25] A. Meetsma, J.L. de Boer, S. van Smaalen, *J. Solid State Chem.* 83 (1989) 370–372.
- [26] Yu. Grin, F.R. Wagner, M. Kohout, M. Armbrüster, A. Leithe-Jasper, U. Wedig, H.G. von Schnering, *J. Solid State Chem.* (2005) accepted for publication.
- [27] W.H. Zachariasen, *Acta Crystallogr.* 1 (1948) 265–268.
- [28] Yu. Grin, U. Wedig, F. Wagner, H.G. von Schnering, A. Savin, *J. Alloys Compd.* 255 (1997) 203–208.
- [29] A.D. Becke, K.E. Edgecombe, *J. Chem. Phys.* 92 (1990) 5397–5403.
- [30] M. Kohout, *Int. J. Quantum Chem.* 97 (2004) 651–658.
- [31] J. Emsley, *The Elements*, Oxford University Press, Oxford, 2000.